# Structural Studies of the System trans-Stilbene/trans-Azobenzene. III. The Structures of Three Mixed Crystals of trans-Azobenzene/trans-Stilbene; Determinations by X-ray and Neutron Diffraction 

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Abstract. $\quad\left(\mathrm{C}_{14} \mathrm{H}_{12}\right)_{X}\left(\mathrm{C}_{12} \mathrm{H}_{10} \mathrm{~N}_{2}\right)_{(1-\chi)}, \quad$ monoclinic, $P 2_{1} / c, Z=4, T=295 \mathrm{~K}$. (I) $X=0 \cdot 26: M_{r}=181 \cdot 71$, $a=15.306$ (2),$\quad b=5.7716$ (4), $\quad c=12.230$ (2) Á, $\beta=112.04(1)^{\circ}, \quad V=1001.5(4) \dot{A}^{3}, \quad D_{x}=$ $1.205 \mathrm{Mg} \mathrm{m}^{-3}, \lambda(\mathrm{Cu} \mathrm{K} \mathrm{\alpha})=1.5418 \AA, \mu=0.47 \mathrm{~mm}^{-1}$, $F(000)=384$, final $R=0.056$ for 1706 unique X-ray data. (II) $X=0.56: \quad M_{r}=181 \cdot 12, \quad a=15.481$ (3), $b=5.749$ (1), $c=12.300(2) \AA, \quad \beta=111.98(1)^{\circ}, \quad V$ $=1015.1(5) \AA^{3}, \quad D_{x}=1.185 \mathrm{Mg} \mathrm{m}^{-3}, \quad \lambda(\mathrm{Mo} K \alpha)=$ $0.71069 \AA, \mu=0.36 \mathrm{~mm}^{-1}, \quad F(000)=384$, final $R$ $=0.051$ for 1586 X-ray data. (III) $X=0.46: M_{r}$ $=181.32, \quad a=15.409(5), \quad b=5.759$ (1), $\quad c=$ 12.284 (4) $\AA, \quad \beta=111.97(3)^{\circ}, \quad V=1010.9$ (7) $\AA^{3}$, $D_{x}=1.191 \mathrm{Mg} \mathrm{m}^{-3}, \quad \lambda=1.304 \AA, \mu=0.186 \mathrm{~mm}^{-1}$, $F(000)=21 \cdot 36$, final $R=0.082$ for 910 neutron reflection data. (IV) $X=0.69: M_{r}=181.72, a=15.548$ (2), $b=5.7388$ (4), $c=12.333$ (2) $\AA, \beta=111.92$ (2) ${ }^{\circ}, V$ $=1020.9(5) \AA^{3}, \quad D_{x}=1.183 \mathrm{Mg} \mathrm{m}^{-3}, \quad \lambda(\mathrm{Mo} \mathrm{K} \mathrm{\alpha})=$ $0.71069 \AA$; no structure determination. The mixed crystals not only exhibit substitutional disorder but both molecules, trans-azobenzene and trans-stilbene, also show configurational disorder at one of the two independent sites with symmetry $\overline{1}$. The structure refinements, in which both kinds of disorder were taken into account, were performed with constraints and restraints. The trans-stilbene molecules show a slight preference for substitution at the disordered sites. This preference can be understood by geometrical considerations.

Introduction. In the course of thermodynamical research into the system trans-azobenzene/transstilbene we have carried out structural studies of some mixed crystals by X-ray and neutron diffraction.

The crystal-structure determinations of the pure substances trans-azobenzene (Brown, 1966) and transstilbene (Hoekstra, Meertens \& Vos, 1975; Finder, Newton \& Allinger, 1974; Bernstein, 1975) led to the suggestion that both trans-stilbene and trans-

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azobenzene show configurational disorder at one of the two independent sites. To solve the structures of the mixed crystals we were in need of a better determination of the mentioned disorder. In part I (Bouwstra, Schouten \& Kroon, 1983) of this series the structure of trans-azobenzene has been redetermined using a model in which the disorder was taken into account. In part II (Bouwstra, Schouten \& Kroon, 1984) the same model was applied to the structure refinement of trans-stilbene. It appeared that both structures show the same kind of disorder and that the molecules at the disordered site are approximately related by a twofold axis. $17 \%$ and $12 \%$ of the molecules trans-azobenzene and trans-stilbene were misoriented. From this it follows that trans-azobenzene and trans-stilbene are not only isostructural but also show the same kind and approximately the same degree of disorder. Moreover the two structures have almost the same packing coefficients (Kitaigorodskii, 1973), which are 0.74 and 0.75 for trans-azobenzene and trans-stilbene respectively. Following Kitaigorodskii these molecules fulfil all conditions to form mixed crystals.

From the literature only a few structural studies on organic mixed crystals are known. In the early seventies Frank, Myasnikova \& Kitaigorodskii (1971) analyzed solid solutions of the system trans-stilbene/diphenylmercury. They found that in the case of solid solutions containing $8 \%$ diphenylmercury these molecules were preferentially substituted at one of the two independent sites. At the same time Frank et al. performed energy calculations on this system. They used a model in which diphenylmercury was infinitely diluted. These calculations confirmed the X-ray studies and indicated that diphenylmercury substituted at one site leads to a lower lattice energy than diphenylmercury substituted at the other site.

The preparation of homogeneous mixed crystalline material has always been a great problem: crystal-
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lization from the melt often leads to inhomogeneities in the solid state due to the low diffusion rate in the solid material. In our group this problem has been solved by the introduction of the zone-levelling technique. Recently we prepared homogeneous mixed single crystals of the system trans-azobenzene/trans-stilbene.

The crystal structures of these mixed crystals are much more complicated than those of the pure components. At both independent sites, i.e. the ordered site (denoted as site $A$ ) and the disordered site (denoted as site $B$ ), trans-azobenzene molecules as well as trans-stilbene molecules can be substituted. This means that site $B$ contains four crystallographically different molecules.

We were particularly interested in the distributions of the stilbene molecules between site $A$ and site $B$. To determine the occupancy of stilbene molecules at both sites we first undertook an X-ray analysis of two mixed crystals containing $26 \%(X=0.26)$ and $56 \%$ ( $X$ $=0.56$ ) stilbene. However, it appeared that the positions of trans-azobenzene and trans-stilbene molecules are very similar. For that reason the percentage stilbene present at site $A$ and site $B$ could not be determined very accurately. Because the $H$ atoms attached to the ethene bond of stilbene are the only atoms that are not closely positioned to azobenzene we decided to use them as probes and deemed it useful to study a mixed crystal ( $X=0.46$ ) by neutron diffraction.

Experimental. Lattice parameters of three mixed crystals (composition: $X=0.26, X=0.56$ and $X$ $=0.69)$ refined by fitting to $\theta, \varphi, \omega$ and $\kappa$ settings of 24 reflections in $\theta$ range 7 to $9^{\circ}$ using Zr -filtered Mo Ka radiation. Lattice parameters of a fourth crystal ( $X=0.46$ ) refined by fitting $2 \theta$ settings of 13 reflections in $\theta$ range 40 to $50^{\circ}$ using neutrons with a wavelength of $1.304 \AA$. Data collection and structure refinement of three mixed crystals, all prepared by the zone-levelling technique, are given separately.
(I) $X=0.26$

Red block-shaped crystals, $0.28 \times 0.30 \times 0.25 \mathrm{~mm}$. Enraf-Nonius CAD-4 diffractometer, Zr -filtered $\mathrm{Cu} K \alpha$ radiation. 7356 reflections measured $\left(2 \theta<70^{\circ}\right.$, $h k l$ range: $h-15-14 ; k-7-7 ; l-18-18)$, 1869 unique reflections ( $R_{\text {int }}=0.041$ ), 1706 reflections with $I>$ $2 \cdot 5 \sigma(I)$ considered observed and included in the refinement. 4 standard reflections measured every 110 reflections; decrease of intensity caused by sublimation was less than $30 \%$; corrections for average change in intensity of reference reflections. Absorption correction ignored. The crystal structure of the mixed crystals is rather complicated (see above). Site $A\left(\frac{1}{2}, 0, \frac{1}{2}\right)$ is filled with trans-stilbene and trans-azobenzene (referred to as $A 1$ and $A 2$ respectively). At site $B(0,0,0)$ four crystallographically different molecules have to be considered: trans-azobenzene and trans-stilbene, both
molecules of which can adopt two orientations (see Fig. 1). We calculated the initial positions of the molecules from the structures of the pure components, leaving the geometry of the molecules intact. Least-squares refinement based on $F$ was carried out using the following model. The benzene rings of the molecules at site $A$ and the benzene rings of both trans-azobenzene and trans-stilbene with the main site occupancy at site $B$ (referred to as $B 1$ and $B 3$ respectively) were refined as rigid bodies. Slack constraints (Waser, 1963) were applied to all exo-ring distances of these molecules. Not the whole molecule was treated as a rigid body because of our interest in the torsion angles in the central part of the molecule. trans-Azobenzene and trans-stilbene with the minor site occupancies at site $B$ (referred to as $B 2$ and $B 4$ ) were fixed in space in view of the low occupancy values. The atoms at approximately the same position were refined with common temperature factors. Moreover, the occupancy ratios of the two orientations of trans-azobenzene (83:17) and transstilbene ( $88: 12$ ) were put equal to those obtained for the pure substances and were fixed during the refinement. Finally the distribution of stilbene molecules over site $A$ and site $B$ was refined keeping the sum of the occupancy values at both sites equal to 1 . In this way the occupancy values are all governed by one variable: $X^{\prime}$, which stands for the fraction of the total amount stilbene present at site $A$. A scheme of the occupancy values is given in Fig. 1.

The initial $R$ was $0 \cdot 15$. During the isotropic least-squares block refinement, which was carried out with a damping factor (Mackay, 1977), it appeared that the distribution of stilbene molecules over the two sites could not be refined probably due to correlation effects between occupancy factors and temperature factors. Therefore we repeated the isotropic refinement with several values of $X^{\prime}$. This yielded a smooth variation in the $R$ value as a function of $X^{\prime}$ as can be inferred from Fig. 2(a). The lowest $R$ was obtained for $X^{\prime}=0 \cdot 30$; corresponding occupancy values are given in Table 1.


Fig. 1. Mixed crystal trans-azobenzene/trans-stilbene ( $X=0.26$ ); example of the scheme of occupancy factors expressed in $X^{\prime}$.

After the isotropic refinement H atoms were introduced for molecules $A 1, A 2, B 1$ and $B 3$. To allow for bond shortening these atoms were placed at a distance $1 \AA$ from their carrier atoms assuming $s p^{2}$ hybridization. The positional parameters of the H atoms were not refined but these atoms 'ride' on their carrier atoms. During the anisotropic refinement the occupancy values corresponding to the lowest $R$ index were used.

After the subsequent anisotropic refinement $R$ dropped to a value of 0.06 . Then the damping factor was removed and the anisotropic thermal parameters of molecules $A 1, B 1, B 2$ and $B 4$ with minor occupancy were replaced by the corresponding $U_{\mathrm{eq}}$, otherwise no convergence could be achieved. The final anisotropic block refinement (with 121 variables, each block containing one molecule) resulted in an $R$ of 0.056 ( $S=0.44$ ); mean $\Delta / \sigma$ and max. $\Delta / \sigma$ were 0.29 and 1.19 respectively. Min. trough and max. peak in final difference Fourier map are -0.21 and $0.23 \mathrm{e} \AA^{-3}$. The positional parameters together with the temperature factors are given in Table 1.*
(II) $X=0.56$

Red block-shaped crystal $(0.20 \times 0.25 \times 0.25 \mathrm{~mm})$, placed in a capillary glass tube to avoid sublimation, which was observed during data collection in case (I). 2762 unique reflections ( $2 \theta<70^{\circ}, h k l$ range: $h$ $-24-24 ; k 0-9 ; \quad l 0-19), 1586$ reflections with $I>2.5 \sigma(I)$ considered observed and included in the refinement. 4 standard reflections measured every 100 reflections; drop of intensity less than $3 \%$. Absorption correction ignored. The initial positions of the molecules were calculated using the structures of the pure components, leaving the geometry of the molecules intact. The refinement was performed with the same model as that applied to the structure of the mixed crystal with $X=0.26$. Again the distribution of stilbene between the two independent sites could not be refined

[^0]due to correlation effects. For that reason the isotropic refinement, which was carried out with a damping factor, was repeated with five values for $X^{\prime}$ (see Fig. $2 b$ ). In this case the lowest $R$ value was obtained for $X^{\prime}=0 \cdot 39$. At this stage of refinement the H atoms were introduced. The occupancy values corresponding to the lowest $R$ value were used and fixed during the subsequent refinement. Then the anisotropic temperature parameters of the atoms belonging to molecules $A 1, B 2, B 3$ and $B 4$ were replaced by their corresponding $U_{\text {eq }}$ parameters and the damping factor was removed. During the succeeding block refinement (with 121 variables, each block containing one molecule) $R$ reduced to a value of 0.051 ( $S=0.57$ ). The final difference map was essentially featureless: min . trough -0.15 and max. peak $0.17 \mathrm{e} \AA^{-3}$. Mean $\Delta / \sigma$ and max. $\Delta / \sigma$ were 0.15 and 0.92 respectively. Final coordinates and temperature factors are collected in Table 1. For the structure determinations of (I) and (II) the scattering factors for N and C were taken from Cromer \& Mann (1968); for H the curve of Stewart, Davidson \& Simpson (1965) was applied.
(III) $X=0.46$

A red irregularly shaped crystal, volume about $10 \mathrm{~mm}^{3}$, was coated with Krylon to avoid sublimation. The neutron data were collected on a four-circle diffractometer at the HFR reactor at Petten. Neutrons with a wavelength of $1.304 \AA$ were obtained after diffraction from the 220 planes of the Cu crystals of a double monochromator. Reflections were measured in the $\omega-2 \theta$ step-scan mode $\left(0.0625^{\circ}\right.$ step $\left.^{-1}\right)$ at room temperature. 1753 unique reflections ( $2 \theta_{\text {max }}=100^{\circ}$, $h k l$ range: $h-15-14 ; k 0-4 ; 10-12), 910$ of which with $F>4 \sigma(F)$ used in least-squares refinement. 2 standard reflections measured every 50 reflections; fluctuations not greater than $2 \%$. Initial positions of the molecules calculated from the structures of the pure substances. The refinement was carried out with the same model as was used in cases (I) and (II). The H atoms were introduced for all molecules before the isotropic refinement was started. These atoms were located at a distance of $1.08 \AA, s p^{2}$ hybridization being assumed. The refinement was performed with a damping factor.


Fig. 2. The $R$ value as a function of $X^{\prime}$. (a) Mixed crystal $X=0.26$. The lowest $R$ value is found for $X^{\prime}=0.30$. (b) Mixed crystal $X=0.56$. The lowest $R$ value corresponds to $X^{\prime}=0 \cdot 39$. (c) Mixed crystal $X=0 \cdot 46$. The minimum in the curve corresponds to $X^{\prime}=0.42$.

$$
U_{\mathrm{eq}}=\frac{1}{3} \sum_{i} \sum_{j} U_{i j} a_{i}^{*} a_{j}^{*} \mathbf{a}_{i} \cdot \mathbf{a}_{j} .
$$

|  | $x$ | y | $z$ |
| :---: | :---: | :---: | :---: |
| (a) Mixed crystal $X=0.26\left(X^{\prime}=0.30\right)$ |  |  |  |
| Molecule $A 1$ (trans-stilbene), occupancy factor $=0.16$ |  |  |  |
| C(1) | 4717 (7) | 883 (12) | 4989 (6) |
| C(2) | 4267 (5) | 1313 (9) | 5841 (6) |
| C(3) | 3738 (5) | 3328 (9) | 5726 (6) |
| C(4) | 3221 (5) | 3724 (9) | 6424 (6) |
| C(5) | 3228 (5) | 2108 (9) | 7258 (6) |
| C(6) | 3761 (5) | 110 (9) | 7398 (6) |
| C(7) | 4276 (5) | -285 (9) | 6704 (6) |

$$
U_{\mathrm{cq}}\left(\mathrm{~A}^{2}\right)
$$

460
434
518
573
577
543
477

Molecule $B 1$ (trans-stilbene), occupancy factor 0.32

| $\mathrm{C}(8)$ | $9661(4)$ | $710(9)$ | $9674(2)$ |
| :--- | ---: | ---: | ---: |
| $\mathrm{C}(9)$ | $9154(3)$ | $595(7)$ | $8388(2)$ |
| $\mathrm{C}(10)$ | $9267(3)$ | $-1243(7)$ | $7712(2)$ |
| $\mathrm{C}(11)$ | $8758(3)$ | $-1284(7)$ | $6497(2)$ |
| $\mathrm{C}(12)$ | $8133(3)$ | $512(7)$ | $5960(2)$ |
| $\mathrm{C}(13)$ | $8020(3)$ | $2350(7)$ | $6637(2)$ |
| $\mathrm{C}(14)$ | $8531(3)$ | $2390(7)$ | $7852(2)$ |

Molecule B2 (trans-stilbene), occupancy factor 0.04

| C(15) | 9908 | -676 | 9529 |
| ---: | ---: | ---: | ---: |
| $\mathrm{C}(16)$ | 9262 | -132 | 8318 |
| $\mathrm{C}(7)$ | 9135 | -1533 | 7347 |
| $\mathrm{C}(18)$ | 8530 | -867 | 6224 |
| $\mathrm{C}(19)$ | 8052 | 1241 | 6072 |
| $\mathrm{C}(20)$ | 8181 | 2661 | 7044 |
| $\mathrm{C}(21)$ | 8784 | 1975 | 8165 |

Molecule A2 (trans-azobenzene), occupancy factor 0.84

| $\mathrm{N}(22)$ | $4893(1)$ | $1032(2)$ | $5041(2)$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{C}(23)$ | $4320(1)$ | $1343(2)$ | $5723(1)$ |
| $\mathrm{C}(24)$ | $3856(1)$ | $3453(2)$ | $5583(1)$ |
| $\mathrm{C}(25)$ | $3295(1)$ | $3909(2)$ | $6220(1)$ |
| $\mathrm{C}(26)$ | $3216(1)$ | $2302(2)$ | $7014(1)$ |
| $\mathrm{C}(27)$ | $3705(1)$ | $-219(2)$ | $7174(1)$ |
| $\mathrm{C}(28)$ | $4259(1)$ | $-281(2)$ | $6525(1)$ |

Molecule B3 (trans-azobenzene), occupancy factor 0.53

| $\mathrm{N}(29)$ | $9721(2)$ | $809(4)$ | $9775(1)$ |
| :--- | ---: | ---: | ---: |
| $\mathrm{C}(30)$ | $9216(2)$ | $582(4)$ | $8529(1)$ |
| $\mathrm{C}(31)$ | $9290(2)$ | $-1294(4)$ | $7852(1)$ |
| $\mathrm{C}(32)$ | $8768(2)$ | $-1324(4)$ | $6640(1)$ |
| $\mathrm{C}(33)$ | $8172(2)$ | $521(4)$ | $6105(1)$ |
| $\mathrm{C}(34)$ | $8099(2)$ | $2398(4)$ | $6783(1)$ |
| $\mathrm{C}(35)$ | $8620(2)$ | $2428(4)$ | $7995(1)$ |

Molecule $B 4$ (trans-azobenzene), occupancy factor 0.1

| $\mathrm{N}(36)$ | 9958 | -734 | 9607 |
| :--- | :--- | ---: | :--- |
| $\mathrm{C}(37)$ | 9286 | -108 | 8474 |
| $\mathrm{C}(38)$ | 9201 | -1637 | 7557 |
| $\mathrm{C}(39)$ | 8631 | -1068 | 6400 |
| $\mathrm{C}(40)$ | 8145 | 1032 | 6160 |
| $\mathrm{C}(41)$ | 8228 | 2560 | 7076 |
| $\mathrm{C}(42)$ | 8798 | 1990 | 8234 |

(b) Mixed crystal $X=0.56\left(X^{\prime}=0.39\right)$

Molecule $A 1$ (trans-stilbene), occupancy factor 0.44

| C(1) | $4737(2)$ | $917(4)$ | $4998(3)$ |
| :--- | :---: | :---: | :---: |
| C(2) | $4242(2)$ | $1330(4)$ | $5793(2)$ |
| C(3) | $3724(2)$ | $3364(4)$ | $5661(2)$ |
| C(4) | $3194(2)$ | $3785(4)$ | $6331(2)$ |
| C(5) | $3179(2)$ | $2176(4)$ | $7155(2)$ |
| C(6) | $3700(2)$ | $159(4)$ | $7312(2)$ |
| C(7) | $4228(2)$ | $-261(4)$ | $6645(2)$ |
| Molecule $B 1$ | (trans-stilbene) | occupancy factor 0.60 |  |
| C(8) | $9713(2)$ | $802(4)$ | $9670(1)$ |
| C(9) | $9169(1)$ | $666(4)$ | $8404(1)$ |
| C(10) | $9248(1)$ | $-1176(4)$ | $7710(1)$ |
| C(11) | $8734(1)$ | $-1162(4)$ | $6506(1)$ |
| C(12) | $8139(1)$ | $692(4)$ | $5996(1)$ |
| C(13) | $8059(1)$ | $2534(4)$ | $6692(1)$ |
| C(14) | $8574(1)$ | $2521(4)$ | $7897(1)$ |

Molecule $B 2$ (trans-stilbene), occupancy factor 0.08

| $\mathrm{C}(15)$ | 9909 | -679 | 9532 |
| ---: | ---: | ---: | ---: |
| $\mathrm{C}(16)$ | 9274 | -132 | 8330 |
| $\mathrm{C}(7)$ | 9179 | -1559 | 7365 |
| $\mathrm{C}(18)$ | 8550 | -870 | 6249 |
| $\mathrm{C}(19)$ | 8078 | 1245 | 6098 |
| $\mathrm{C}(20)$ | 8205 | 2672 | 7064 |
| $\mathrm{C}(21)$ | 8803 | 1983 | 8179 |

589
527
604
655
652
686
626
490
453
534
596
600
584
507

$596(13)$
$523(1)$
$591(13)$
$637(14)$
$625(13)$
$699(15)$
$646(13)$

Molecule A2 (trans-azobenzene), occupancy factor 0.56

| $\mathrm{N}(22)$ | $4893(2)$ | $1029(2)$ | $5051(2)$ | $495(9)$ |
| :--- | ---: | ---: | ---: | :--- |
| $\mathrm{C}(23)$ | $4313(1)$ | $1318(3)$ | $5716(2)$ | $455(0)$ |
| $\mathrm{C}(24)$ | $3850(1)$ | $3428(3)$ | $5574(2)$ | $553(13)$ |
| $\mathrm{C}(25)$ | $3299(1)$ | $3885(3)$ | $6213(2)$ | $621(14)$ |
| $\mathrm{C}(26)$ | $3230(1)$ | $2277(3)$ | $7010(2)$ | $629(15)$ |
| $\mathrm{C}(27)$ | $3718(1)$ | $193(3)$ | $7173(2)$ | $598(14)$ |
| $\mathrm{C}(28)$ | $4262(1)$ | $-307(3)$ | $6521(2)$ | $515(12)$ |

Molecule B3 (trans-azobenzene), occupancy factor 0.26

| $\mathrm{N}(29)$ | $9678(3)$ | $714(8)$ | $9777(1)$ | 589 |
| :--- | ---: | ---: | ---: | ---: |
| $\mathrm{C}(30)$ | $9218(3)$ | $484(6)$ | $8536(1)$ | 515 |
| $\mathrm{C}(31)$ | $9307(3)$ | $-1439(6)$ | $7896(1)$ | 580 |
| $\mathrm{C}(32)$ | $8802(3)$ | $-1540(6)$ | $6690(1)$ | 617 |
| $\mathrm{C}(33)$ | $8209(3)$ | $282(6)$ | $6124(1)$ | 609 |
| $\mathrm{C}(34)$ | $8119(3)$ | $2205(6)$ | $6766(1)$ | 671 |
| $\mathrm{C}(35)$ | $8625(3)$ | $2306(6)$ | $7972(1)$ | 638 |

Molecule $B 4$ (trans-azobenzene), occupancy factor 0.06

| $\mathrm{N}(36)$ | 9930 | -773 | 9620 | 589 |
| :--- | ---: | ---: | ---: | ---: |
| $\mathrm{C}(37)$ | 9295 | -109 | 8484 | 515 |
| $\mathrm{C}(38)$ | 9211 | -1643 | 7572 | 580 |
| $\mathrm{C}(39)$ | 8648 | -1072 | 6423 | 609 |
| $\mathrm{C}(40)$ | 8168 | 1037 | 6148 | 617 |
| $\mathrm{C}(41)$ | 8249 | 2570 | 7095 | 671 |
| C(42) | 8813 | 1998 | 8245 | 638 |

(c) Mixed crystal $X=0.46\left(X^{\prime}=0.42\right)$

464 (7) Molecule $A 1$ (trans-stilbene), occupancy factor 0.37

| $431(8)$ | $\mathrm{C}(1)$ | $4724(9)$ | $887(14)$ | $4999(8)$ | $426(12)$ |
| :--- | :--- | :---: | :---: | :---: | :---: |
| $526(10)$ | $\mathrm{C}(2)$ | $4281(5)$ | $1302(9)$ | $5854(6)$ | $373(13)$ |
| $581(11)$ | $\mathrm{C}(3)$ | $3727(5)$ | $3273(9)$ | $5722(6)$ | $444(14)$ |
| $561(11)$ | $\mathrm{C}(5)$ | $3202(5)$ | $3623(9)$ | $6408(6)$ | $429(15)$ |
| $546(10)$ | $\mathrm{C}(4)$ | $3225(5)$ | $2006(8)$ | $7246(5)$ | $49(17)$ |
| $477(9)$ | $\mathrm{C}(6)$ | $3783(5)$ | $56(9)$ | $7407(6)$ | $409(13)$ |
|  | $\mathrm{C}(7)$ | $4306(5)$ | $-296(9)$ | $6721(6)$ | $399(13)$ |
| $583(14)$ | Molecule $B 1($ trans-stilbene $)$, | occupancy factor 0.46 |  |  |  |
| $531(15)$ | $\mathrm{C}(8)$ | $9689(11)$ | $788(19)$ | $9692(3)$ | $547(14)$ |
| $615(17)$ | $\mathrm{C}(9)$ | $9153(4)$ | $733(8)$ | $8417(2)$ | $501(15)$ |
| $657(19)$ | $\mathrm{C}(10)$ | $9255(4)$ | $-1048(8)$ | $7704(2)$ | $459(16)$ |
| $651(9)$ | $\mathrm{C}(11)$ | $8729(4)$ | $-1021(8)$ | $6500(2)$ | $477(16)$ |
| $674(19)$ | $\mathrm{C}(12)$ | $8102(4)$ | $789(8)$ | $6009(2)$ | $479(16)$ |
| $638(18)$ | $\mathrm{C}(13)$ | $8001(4)$ | $2571(8)$ | $6721(2)$ | $542(16)$ |
|  | $\mathrm{C}(14)$ | $8526(4)$ | $2544(8)$ | $7925(2)$ | $563(16)$ |

Molecule $B 2$
$\mathrm{C}(15)$
$\mathrm{C}(16)$
$\mathrm{C}(17)$
$\mathrm{C}(18)$
$\mathrm{C}(19)$
$\mathrm{C}(20)$
$\mathrm{C}(21)$

Molecule $A 2$ (trans-azobenzene), occupancy factor 0.63

| N (22) | 4900 (3) | 1035 (2) | 5048 (5) | 426 (12) |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{C}(23)$ | 4301 (3) | 1356 (6) | 5686 (4) | 373 (13) |
| $\mathrm{C}(24)$ | 3855 (3) | 3490 (6) | 5547 (4) | 443 (14) |
| $\mathrm{C}(25)$ | 3300 (3) | 3981 (6) | 6180 (4) | 429 (15) |
| $\mathrm{C}(26)$ | 3209 (3) | 2382 (6) | 6969 (4) | 495 (17) |
| $\mathrm{C}(27)$ | 3681 (3) | 274 (6) | 7128 (4) | 409 (13) |
| C(28) | 4222 (3) | -258(6) | 6482 (4) | 399 (13) |
| Molecule $B 3$ (trans-azobenzene), occupancy factor 0.39 |  |  |  |  |
| N (29) | 9724 (9) | 803 (15) | 9752 (2) | 547 (14) |
| $\mathrm{C}(30)$ | 9234 (5) | 468 (8) | 8522 (2) | 501 (15) |
| $\mathrm{C}(31)$ | 9308 (5) | -1517 (8) | 7911 (2) | 459 (16) |
| $\mathrm{C}(32)$ | 8809 (5) | -1668 (8) | 6704 (2) | 477 (16) |
| $\mathrm{C}(33)$ | 8236 (5) | 162 (8) | 6107 (2) | 479 (16) |
| C(34) | 8160 (5) | 2146 (8) | 6717 (2) | 542 (16) |
| C(35) | 8660 (5) | 2299 (8) | 7924 (2) | 563 (16) |
| Molecule $B 4$ (trans-azobenzene), occupancy factor 0.08 |  |  |  |  |
| N(36) | 9915 | -772 | 9612 | 438 |
| C(37) | 9280 | -110 | 8479 | 334 |
| $\mathrm{C}(38)$ | 9202 | -1641 | 7566 | 465 |
| $\mathrm{C}(39)$ | 8641 | -1067 | 6414 | 466 |
| $\mathrm{C}(40)$ | 8155 | 1035 | 6174 | 474 |
| C(41) | 8233 | 2566 | 7086 | 447 |
| $\mathrm{C}(42)$ | 8796 | 1994 | 8238 | 376 |

Although neutron scattering of H is more pronounced than X-ray scattering of H and in addition the positions of the H atoms of trans-azobenzene and trans-stilbene molecules are less similar than that of the non-hydrogen atoms, it appeared that the distribution of trans-stilbene between site $A$ and site $B$ could not be refined. So the isotropic refinement was again carried out with several values for $X^{\prime}$. As is shown in Fig. 2(c) the lowest $R$ value $(0.148)$ was obtained with $X^{\prime}=0.42$. The occupancy factors are given in Table 1. At this stage an absorption correction was applied: we preferred an empirical absorption correction due to the irregular shape of the crystal. The absorption correction was carried out with DIFABS (Walker \& Stuart, 1983). Anisotropic block refinement started at an $R$ value of $0 \cdot 141$. In contrast to the preceding refinement the H atoms were refined anisotropically. During the final stage of refinement the anisotropic thermal parameters of molecules $B 2$ and $B 4$ were replaced by the corresponding $U_{\text {eq. }} . R$ dropped to 0.082 ; the number of variables was 193 ( $R_{w}=0.072, S=0.39$ ). Mean $\Delta / \sigma$ and max. $\Delta / \sigma$ are 0.15 and 0.83 respectively. In the final difference map max. peak and min. trough were 0.10 and $-0.09 \mathrm{fm} \AA^{-3}$ respectively. The neutron scattering lengths used for $\mathrm{C}, \mathrm{N}$ and H are $0.665,0.94$ and -0.374 fm .

Calculations carried out on the CDC-Cyber 175 computer of the University of Utrecht with SHELX76 (Sheldrick, 1976) and programs of the $A P O L L O$ (data reduction and corrections; A. L. Spek) and EUCLID (calculation of geometrical data and illustrations; Spek, 1982) packages.

Discussion. From Fig. 3 it can be seen that the lattice parameters of the mixed crystals almost obey Vegard's Law. Consequently the excess volume of these crystals is almost zero.

A survey of the bond distances and bond angles obtained, together with their constrained values, is given in Table 2.

In Table 3 the relevant torsion angles, that were not constrained, are shown; the molecules at both independent sites prefer an almost planar conformation. From


Fig. 3. Graph of the unit-cell volume as a function of the mole fraction ( $X$ ) of trans-stilbene.

Table 2. Bond distances $(\AA)$ and bond angles $\left(^{\circ}\right)$ in the mixed crystals with occasional restraints imposed during the refinement

Molecules $B 2$ and $B 4$ are not included. Superscripts indicate symmetry-related units according to the following code: (i) $1-x$, $-y, 1-z$; (ii) $2-x,-y, 2-z$.

|  | $X=0.26$ | $X=0.56$ | $X=0.46$ | Restraint |
| :---: | :---: | :---: | :---: | :---: |
| Molecule $A 1^{*}$ |  |  |  |  |
| $\mathrm{C}(1)-\mathrm{C}\left(1{ }^{\text {i }}\right.$ ) | 1.331 (12) | 1.331 (4) | 1.329 (14) | 1.33 |
| C(1)-C(2) | 1.470 (12) | 1.470 (5) | 1.471 (14) | 1.471 |
| $\mathrm{C}(2)-\mathrm{C}(1)-\mathrm{C}\left(1^{\mathrm{i}}\right)$ | 126.1 (7) | 126.6 (3) | $126 \cdot 3$ (9) | 126.1 |
| $\mathrm{C}(1)-\mathrm{C}(2)-\mathrm{C}(3)$ | 118.6 (6) | 118.6 (2) | 118.5 (7) | 118.6 |
| $\mathrm{C}(1)-\mathrm{C}(2)-\mathrm{C}(7)$ | 123.3 (6) | 122.5 (5) | 123.3 (6) | 123.2 |
| Mean intraring bond length | 1.389 (7) | 1-389 (7) | 1.389 (7) |  |
| Mean intraring bond angle | 120 (1) | 120 (1) | 120 (1) |  |
| Molecule A2* |  |  |  |  |
| $\mathrm{N}(22)-\mathrm{N}\left(22^{\text {i }}\right.$ ) | 1.249 (2) | 1.248 (2) | $1 \cdot 248$ (3) | 1.250 |
| $\mathrm{N}(22)-\mathrm{C}(23)$ | 1.431 (3) | 1.433 (4) | 1.429 (8) | 1.429 |
| $\mathrm{N}\left(22^{\text {i }}\right)-\mathrm{N}(22)-\mathrm{C}(23)$ | 113.7 (2) | 114.5 (2) | $114 \cdot 1$ (4) | 113.8 |
| $\mathrm{N}(22)-\mathrm{C}(23)-\mathrm{C}(24)$ | $115 \cdot 8$ (1) | 115.8 (2) | 116.1(4) | 116.2 |
| $\mathrm{N}(22)-\mathrm{C}(23)-\mathrm{C}(28)$ | 123.2 (1) | 123.1 (2) | 123.0 (3) | 122.9 |
| Mean intraring bond length | 1.387 (4) | 1.386 (4) | $1 \cdot 386$ (3) |  |
| Mean intraring bond angle | $120 \cdot 0$ (7) | $120 \cdot 0$ (7) | $120 \cdot 0$ (7) |  |
| Molecule B1† |  |  |  |  |
| $\mathrm{C}\left(8^{\text {li }}\right)-\mathrm{C}(8)$ | $1 \cdot 330$ (8) | 1.326 (4) | 1.331 (19) | 1.330 |
| $\mathrm{C}(8)-\mathrm{C}(9)$ | 1.471 (5) | 1.469 (3) | 1.473 (11) | 1.471 |
| $\mathrm{C}\left(8^{\text {17 }}\right)-\mathrm{C}(8)-\mathrm{C}(9)$ | 126.4 (4) | 126.8 (2) | $126 \cdot 0$ (8) | 126.1 |
| $\mathrm{C}(8)-\mathrm{C}(9)-\mathrm{C}(10)$ | 122.5 (4) | 122.9 (2) | $122 \cdot 2$ (6) | 122.4 |
| $\mathrm{C}(8)-\mathrm{C}(9)-\mathrm{C}(14)$ | 117.6 (4) | 117.0 (2) | 117.8 (6) | 117.5 |
| Molecule B3† |  |  |  |  |
| $\mathrm{N}(29 \mathrm{ii})-\mathrm{N}(29)$ | 1.246 (4) | 1-249 (6) | 1.250 (15) | 1.25 |
| $\mathrm{N}(29)-\mathrm{C}(30)$ | 1.432 (3) | 1.429 (4) | 1.427 (10) | 1.429 |
| $\mathrm{N}(29 \mathrm{i})-\mathrm{N}(29)-\mathrm{C}(30)$ | 114.1 (2) | 113.9 (3) | $114 \cdot 2$ (7) | 113.8 |
| $\mathrm{N}(29)-\mathrm{C}(30)-\mathrm{C}(31)$ | 124.8 (2) | 124.2 (3) | 124.3 (6) | 121.3 |
| $\mathrm{N}(29)-\mathrm{C}(30)-\mathrm{C}(35)$ | 115.2 (2) | 115.7 (3) | 115.8 (5) | 116.2 |

* Intraring bond angles and intraring bond lengths are put equal to those of the pure components and fixed during the refinement; numbers in parentheses refer to standard deviations in the mean of the values used.
$\dagger$ Intraring bond angles $120^{\circ}$; intraring bond lengths $1.395 \AA$.

Table 3. Selected torsion angles $\left({ }^{\circ}\right)$ of molecules $A 1$, $A 2, B 1$ and $B 3$ with their e.s.d.'s in parentheses


Table 1 it can be inferred that the thermal motion at site $B$ is larger than that at site $A$ probably due to more available space at site $B$. This difference in thermal motion is also observed in the crystals of the pure substances. The relatively high $R$ value found for the crystal with $X=0.46$ is probably due to the large number of H atoms: during neutron diffraction these atoms cause incoherent neutron background scattering. Moreover, the mixed crystal used was of minimal size which caused a data set with predominantly weak intensities.

In Fig. 4(a) trans-azobenzene and trans-stilbene at site $A$ are drawn. From this figure it is clear that these molecules almost overlap. In Figs. $4(b)$ and 4(c) ORTEP drawings (Johnson, 1971) of the disordered molecules of trans-azobenzene and trans-stilbene at site $B$, along with their numbering scheme, are shown. It can be concluded that the molecules at site $B$ show the same kind of disorder as that of the pure components. From Fig. $4(b)$ it is clear that the H atoms attached to the ethene bond of stilbene are the only atoms which do not overlap with azobenzene atoms. To determine more accurately the distribution of stilbene a difference Fourier map was calculated in which these H atoms were not included in the structure factor calculations. The intensity data for the mixed crystal with $X=0.46$ were used because the neutron scattering of H is larger than the X-ray scattering of H . Since the positions of $\mathrm{H}(8)$ and $\mathrm{H}\left(15^{\mathrm{ii}}\right)$ are very similar (see Fig. $4 c$ ) this difference map exhibits two maxima: one at the position of $\mathbf{H}(1)$ and a second higher maximum at the positions of $\mathbf{H}(8)$ and $\mathbf{H}\left(15^{\text {ii }}\right.$ ) (see Fig. 5). Integration of these two peaks results in a density ratio of $64: 36$, which indicates that $36 \%$ of the total amount of stilbene is added at site $A$. This agrees very well with the distributions of stilbene molecules corresponding to the lowest $R$ values obtained by the isotropic refinement (see Table 1). So it might be concluded that transstilbene is preferentially substituted at site $B$. As is mentioned before, site $B$ has more available space than site $A$ ( 256 vs $252 \AA^{3}$ respectively). With van der Waals radii the volumes of trans-azobenzene and transstilbene are 172 and $180 \AA^{3}$ respectively. Comparison of these values, which are calculated with SPACE (Schreurs \& Spek, 1985), leads to the conclusion that the larger stilbene molecule is preferentially substituted at site $B$ which takes up the greater volume. It is intended to supplement these findings, which in spite of some experimental and refinement problems are fairly conclusive, with atom-atom potential calculations.

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Fig. 4. (a) A composite view of molecules $A 1$ (trans-stilbene) and A2 (trans-azobenzene) in the mixed crystal $X=0.56$. $50 \%$ probability plots of thermal ellipsoids of molecules $A 1$ and $A 2$. (b) View of disordered molecules $B 3$ and $B 4$ in the mixed crystal $X=0.56$. (c) A composite view of the disordered stilbene molecules at site $B$ of the mixed crystal $X=0.46$. $50 \%$ probability plots for thermal ellipsoids of molecule $B 1$.


Fig. 5. A difference electron density map of the mixed crystal ( $X=0.46$ ) drawn with $S P A C E$ (Schreurs \& Spek, 1985). The H atoms belonging to the ethene moiety of trans-stilbene are not included in $F_{c}$. A: peak located at the position of $\mathrm{H}(1) . B$ : peak located at the positions of $\mathrm{H}(8)$ and $\mathrm{H}\left(15^{\mathrm{ii}}\right)$.

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# cis-6,11,17,18-Tetrahydro-5,12-dioxatribenzo[a,e,i]cyclododecene-17,18-diol, $\mathrm{C}_{22} \mathrm{H}_{20} \mathrm{O}_{4}$ 

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#### Abstract

M_{r}=348.4\), triclinic, $P \overline{1}, \quad a=8.633$ (1), $b=9.035$ (1),$\quad c=11.957$ (1) $\AA, \quad \alpha=74.11$ (1),$\quad \beta=$ 73.61 (1), $\quad \gamma=83.00(1)^{\circ}, \quad V=859.5$ (2) $\AA^{3}, \quad Z=2$, $D_{x}=1.346 \mathrm{~g} \mathrm{~cm}^{-3}, \quad \lambda=0.71073 \AA, \quad \mu($ Mo $K \alpha)=$ $0.86 \mathrm{~cm}^{-1}, F(000)=368 \cdot 0, T=296 \mathrm{~K}, R=0.031$ for 2016 observations (of 3010 unique data). The diol O atoms form a gauche interaction with $\mathrm{O}-\mathrm{C}-\mathrm{C}-\mathrm{O}$ torsion angle, $42.5(3)^{\circ}$, smaller than that in related compounds. Both intramolecular and intermolecular hydrogen bonding are present.


Introduction. During the course of our studies preparing stilbene cycles as backbones for intramolecular reactions (Tirado-Rives, Oliver, Fronczek \& Gandour, 1984), the title compound has been isolated and its crystal structure has been determined.

Experimental. Title compound isolated from mixture produced in the reaction of $2,2^{\prime}-[o$-phenylenebis(methyleneoxy)]dibenzaldehyde with $\mathrm{TiCl}_{4} / \mathrm{BuLi}$. Colorless plates from evaporation of $\mathrm{CHCl}_{3}$, m.p. $455-458 \mathrm{~K}$. $D_{m}$ not determined. Crystal size $0.20 \times 0.42 \times$ 0.60 mm . Space-group determination by successful refinement of centrosymmetric model. Cell dimensions from setting angles of 25 reflections having $13^{\circ}>$ $\theta>12^{\circ}$. Data collection on Enraf-Nonius CAD-4 diffractometer, Mo $K \alpha$ radiation, graphite monochromator, $\omega-2 \theta$ scans designed for $I=50 \sigma(I)$. Scan rates varied $0.57-20.0^{\circ} \mathrm{min}^{-1}$. Reflections having $1^{\circ}<\theta<25^{\circ}, 0 \leq h \leq 10,-10 \leq k \leq 10,-13 \leq l \leq 13$ (excluding redundant data) measured, corrected for background, Lorentz, and polarization effects. Maximum value of $(\sin \theta) / \lambda=0.59 \AA^{-1}$. Three standard reflections, $\pm 1.6 \%$ random variation. Absorption negli-

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gible. Structure solved using MULTAN78 (Main, Hull, Lessinger, Germain, Declercq \& Woolfson, 1978), refined by full-matrix least squares based upon $F$, using data for which $I>3 \sigma(I)$ (994 unobserved reflections), weights $w=\sigma^{-2}\left(F_{o}\right)$, with the EnrafNonius SDP (Frenz \& Okaya, 1980). Non-H atoms anisotropic; H atoms located by $\Delta F$ synthesis and refined isotropically. Final $R=0.031, R_{w}=0.043$, $S=1.413$ for 316 variables. Maximum shift $0.02 \sigma$ in final cycle, largest residual density $0 \cdot 16 \mathrm{e} \AA^{-3}$, extinction coefficient $3.0(3) \times 10^{-6}$.

Discussion. The atomic parameters are given in Table 1. $\dagger$ Selected torsion angles are given in Fig. 1.

There are some noteworthy values for the angles and torsion angles associated with the diol C atoms. The angles, $C(9)-C(8)-C(7)$ and $C(6)-C(7)-C(8)$, are $115.4(1)$ and $115.6(1)^{\circ}$, respectively, which are significant distortions from their expected tetrahedral values. The torsion angles about $C(7)-C(8)$ are surprising in that the gauche interactions are nearly $20^{\circ}$ less than the typical values. This conformation brings the two hydroxyl O atoms within 2.689 (1) $\AA$ of each other. While no torsional motion about $C(7)-C(8)$ can produce a linear intramolecular hydrogen bond, the observed twist brings the H atom on $\mathrm{O}(3)$ to a position equidistant from the plane defined by $\mathrm{C}(7), \mathrm{O}(3)$, and $\mathrm{O}(4)$, and the plane bisecting the $\mathrm{C}(8)-\mathrm{O}(4)-\mathrm{H}(40)$ angle: 0.35 (2) $\AA$ from each. The $\mathrm{O}(3)-\mathrm{H}(30) \cdots \mathrm{O}(4)$
$\dagger$ Tables of distances and angles, H -atom coordinates. H -atom distances and angles, anisotropic thermal parameters, deviations from least-squares planes, and structure factor amplitudes have been deposited with the British Library Lending Division as Supplementary Publication No. SUP 39872 (19 pp.). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CHI 2HU, England.
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[^0]:    * Lists of structure factors, anisotropic thermal parameters and H -atom parameters for all three compounds have been deposited with the British Library Lending Division as Supplementary Publication No. SUP 39850 (31 pp.). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CHI 2HU, England.

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